

3. EXAMPLE 1: SPRING PENDULUM (DOF: 2)

In Fig. 1 the sketch of spring pendulum can be seen.

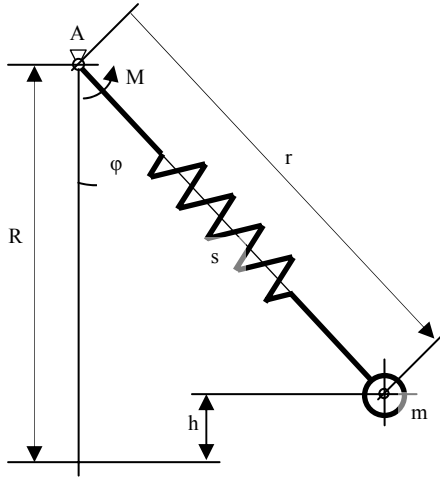


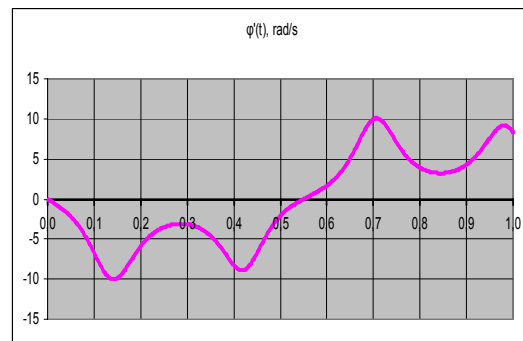
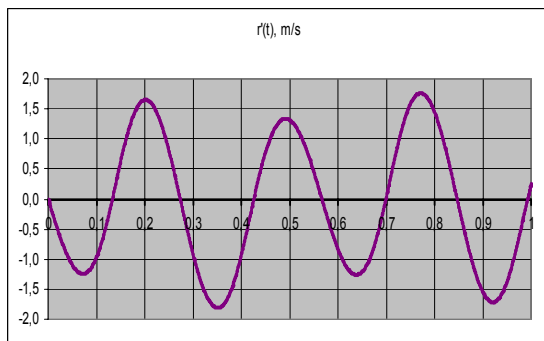
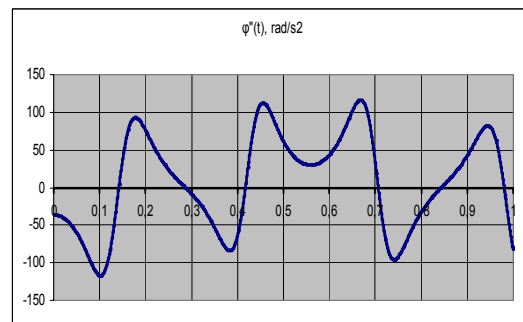
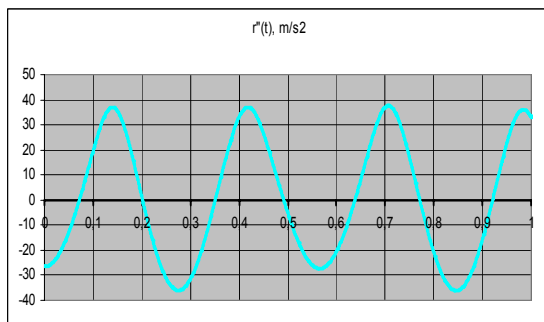
Figure 1
Sketch of spring pendulum

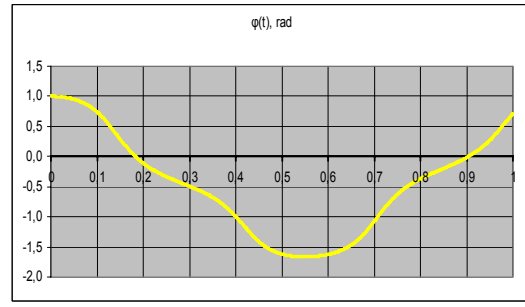
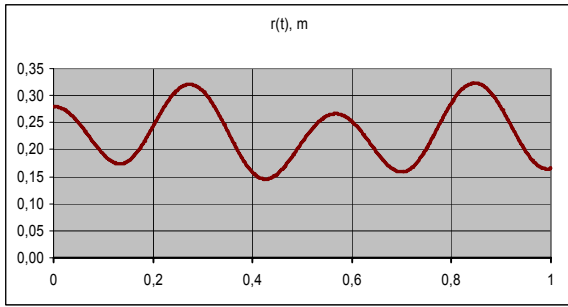
Data:
 $M = -1 \text{ Nm}$, $s = 800 \text{ N/m}$
 $m = 2 \text{ kg}$
 $R = 0,2 \text{ m}$ (length of unloaded rod)
 $g = 10 \text{ m/s}^2$
 $\dot{r}_o = 0 \text{ m/s}$, $r = 0,28 \text{ m}$
 $\dot{\varphi}_o = 0 \text{ rad/s}$, $\varphi_o = 1 \text{ rad}$
 (time step: 0.0001 s,
 time interval: $0 \leq t \leq 1 \text{ s}$)

The motion of the spring pendulum is described by the following second order differential equation system. They can be obtained by the aid of second order Lagrangian-equation.

$$\ddot{r} = \frac{m r \dot{\varphi}^2 - s(r - r_o) + m g \cos \varphi}{m}, \quad \ddot{\varphi} = \frac{M - m g r \sin \varphi - 2 m r \dot{\varphi}}{m r^2}$$

After two-time numerical integration of motion equations the following kinematical functions can be obtained.





4. EXAMPLE 2: LINK MECHANISM WITH RECIPROCATING MOTION MASS (DOF: 2)

In Fig. 2 a sketch of a simple mechanical system (two degrees of freedom) can be seen. There is a mass and a link mechanism in between a spring.

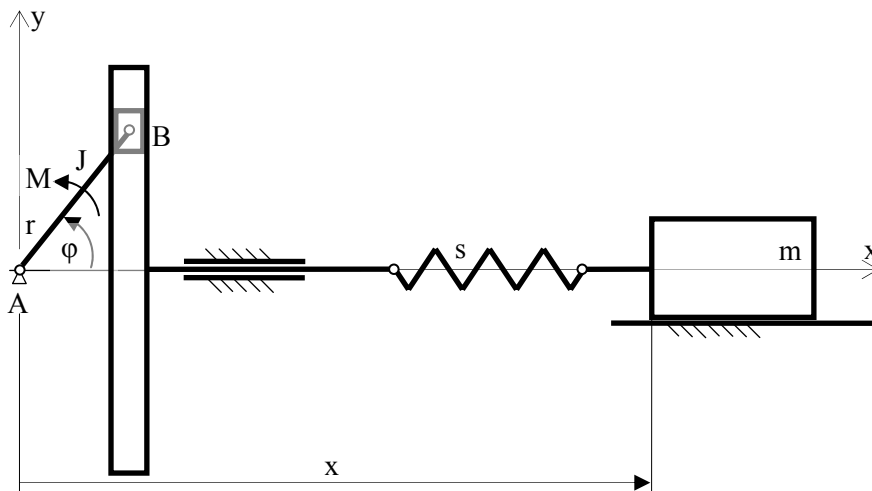
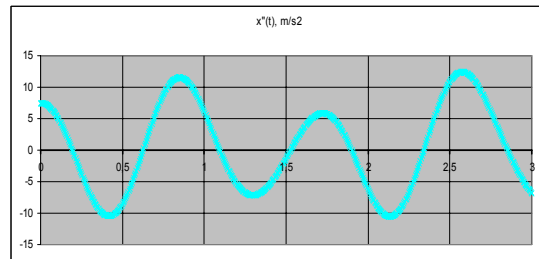
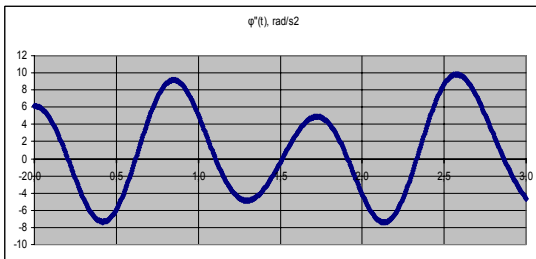


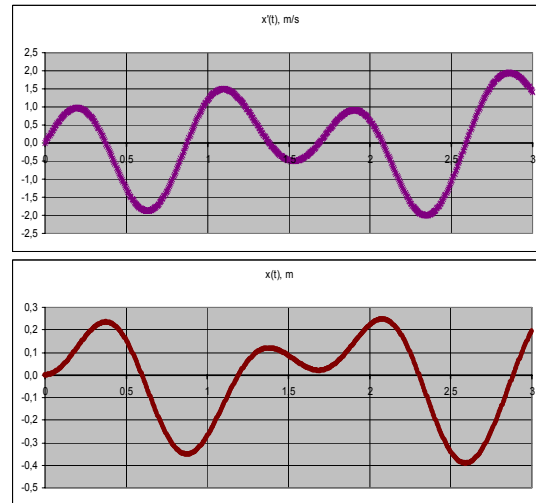
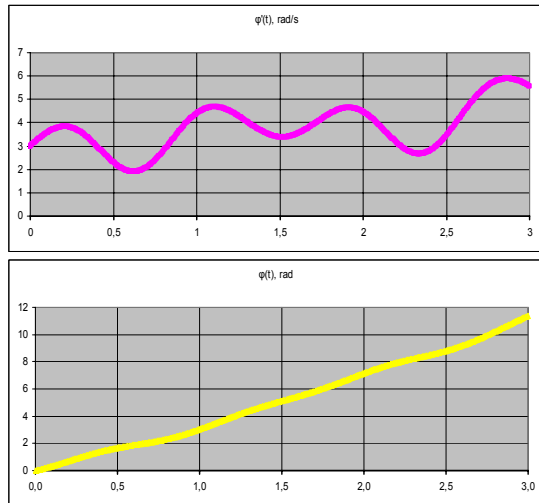
Figure 2 Sketch of link mechanism

Data: $M = 2 \text{ Nm}$, $J = 4 \text{ kgm}^2$, $r = 0.15 \text{ m}$, $s = 1000 \text{ N/m}$, $m = 20 \text{ kg}$, $\dot{x}_o = 0 \text{ m/s}$, $x_o = 0 \text{ m}$, $\dot{\phi}_o = 3 \text{ rad/s}$, $\phi_o = 0 \text{ rad}$, (time step: 0.005 s, time interval: $0 \leq t \leq 3 \text{ s}$). The motion of the link mechanism can be described by the following second order differential equation system.

$$\ddot{r} = \frac{sr \cos \phi - k\dot{x} - sx}{m}, \quad \ddot{\phi} = \frac{M - sr(x - r \cos \phi)}{J}$$

After two-time numerical integration of motion equations the kinematical functions will be the followings.





5. CONCLUSION

The above demonstrated method can be applied easily for engineer students in the higher education. The method is suitable for investigation of similar mechanical systems having one or more degrees of freedom. By consequent modification of data (physical quantities) of systems a wide range of possible structures and their kinematical behavior can be analyzed. For this reason the application of this method can be advantageous for engineer students.

REFERENCES

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